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# A Si IV/O IV Electron Density Diagnostic for the Analysis of *IRIS* Solar Spectra

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## Abstract

Solar spectra of ultraviolet bursts and flare ribbons from the *Interface Region Imaging Spectrograph* (*IRIS*) have suggested high electron densities of  $>10^{12} \text{ cm}^{-3}$  at transition region temperatures of 0.1 MK, based on large intensity ratios of Si IV  $\lambda 1402.77$  to O IV  $\lambda 1401.16$ . In this work, a rare observation of the weak O IV  $\lambda 1343.51$  line is reported from an X-class flare that peaked at 21:41 UT on 2014 October 24. This line is used to develop a theoretical prediction of the Si IV  $\lambda 1402.77$  to O IV  $\lambda 1401.16$  ratio as a function of density that is recommended to be used in the high-density regime. The method makes use of new pressure-dependent ionization fractions that take account of the suppression of dielectronic recombination at high densities. It is applied to two sequences of flare kernel observations from the October 24 flare. The first shows densities that vary between  $3 \times 10^{12}$  and  $3 \times 10^{13} \text{ cm}^{-3}$  over a seven-minute period, while the second location shows stable density values of around  $2 \times 10^{12} \text{ cm}^{-3}$  over a three-minute period.

**Key words:** Sun: activity – Sun: transition region – Sun: UV radiation

## 1. Introduction

The *Interface Region Imaging Spectrograph* (*IRIS*; De Pontieu et al. 2014) observes four of the five O IV intercombination lines between 1399 and 1405 Å, and the two resonance lines of Si IV at 1393.76 and 1402.77 Å, which together diagnose the solar transition region around 0.1 MK. The O IV lines are well known to form density diagnostics that are valuable for solar and stellar spectroscopists (e.g., Keenan et al. 2002). However, at high electron number densities of  $N_e > 10^{12} \text{ cm}^{-3}$ , the O IV diagnostics lose sensitivity and so are no longer useful. It was noted by Feldman et al. (1977) that the O IV lines become very weak relative to the Si IV lines in flare spectra, which was interpreted as collisional de-excitation becoming the dominant de-population method for the O IV lines' upper levels at high densities, thus reducing their photon yields in comparison to the Si IV resonance lines. The ratio of a Si IV line to a O IV line can thus be used as a density diagnostic in the regime  $N_e > 10^{12} \text{ cm}^{-3}$  that is not otherwise accessible by *IRIS*. Feldman et al. (1977) constructed a method for interpreting the ratio that yielded a value of  $>10^{13} \text{ cm}^{-3}$  for one *Skylab* solar flare observation, and similar results were presented by later authors—see Doschek et al. (2016) for a review of results from the *Skylab* and Solar Maximum Mission experiments.

After the launch of *IRIS* in 2013 there has been renewed interest in the use of Si IV and O IV to derive densities, particularly with regard to intense transition region bursts that occur within active regions. These ultraviolet (UV) bursts demonstrate very strong Si IV emission and also weak or non-existent O IV emission. Peter et al. (2014) presented four examples that they named “bombs,” and which exhibited lower limits of 50–350 for the Si IV  $\lambda 1402.77$  to O IV  $\lambda 1401.16$  ratio, which compare with a value of around 4 in quiet Sun (QS) conditions (Doschek & Mariska 2001). Tian et al. (2016) studied 10 UV bursts and found ratios ranging from 32 to 498

for 8 of the events, but also 2 that had low ratios of 7. They inferred that the ratios (and thus densities) are sensitive to the heights of formation of the bursts. To convert measured ratios to densities, Peter et al. (2014) created a constant pressure model for the line emissivities, and this yielded densities of  $\gtrsim 10^{13} \text{ cm}^{-3}$  for the four UV bursts studied in this work. This method was also applied by Kim et al. (2015), Yan et al. (2015), and Gupta & Tripathi (2015) to other UV bursts, and similar high densities were found. The high densities found for the UV bursts were cited by Peter et al. (2014) as evidence for their formation in the temperature minimum region (500 km above the solar surface) or lower. However, Judge (2015) questioned the Peter et al. (2014) result, citing uncertainties in element abundances, temperature structure, and atomic data, and they argued that the UV bursts are likely formed in a lower density regime that is higher in the atmosphere. Despite these concerns, a single density–ratio relationship for Si IV and O IV is very appealing due to the paucity of other *IRIS* diagnostics in the high-density regime, as demonstrated by the use of the method in Kim et al. (2015), Yan et al. (2015), Gupta & Tripathi (2015), and Polito et al. (2016). For this reason, we re-visit the Si IV-to-O IV ratio method here.

Judge (2015) recommended that the O IV allowed multiplet around 1340 Å (two lines at 1338.61 and 1343.51 Å) be included in the *IRIS* analysis, but these wavelengths are often not downloaded due to *IRIS* telemetry restrictions. Even when the wavelengths are downloaded, the lines are usually too weak to observe. For the present work, we utilize a flare data set where  $\lambda 1343.51$  is observed and automatic exposure control reduces the exposure time by a factor of more than 30, thus enabling reliable intensity estimates for the O IV and Si IV lines. This allows the Si IV–O IV density diagnostic method to be investigated, and also for the method to be benchmarked against the usual intercombination line density diagnostic.

Section 2 describes the atomic data and emission line modeling technique used in the present work. A method for creating a Si IV

**Table 1**  
Emission Lines Studied in the Present Work

Ion	$\log(T_{\max}/\text{K})$	Wavelength/ $\text{\AA}$	Transition	$\log(T_{\text{mem}}/\text{K})$
O IV	5.17	1343.51	$2s2p^2\ ^2P_{3/2}-2p^3\ ^2D_{5/2}$	5.15
		1399.78	$2s^22p\ ^2P_{1/2}-2s2p^2\ ^4P_{1/2}$	5.09
		1401.16	$2s^22p\ ^2P_{3/2}-2s2p^2\ ^4P_{5/2}$	5.09
		1404.78	$2s^22p\ ^2P_{3/2}-2s2p^2\ ^4P_{3/2}$	5.09
Si IV	4.88	1393.76	$3s\ ^2S_{1/2}-3p^2P_{3/2}$	4.85
		1402.77	$3s^2\ S_{1/2}-3p\ ^2P_{3/2}$	4.85
S IV	4.98	1404.83	$3s^23p\ ^2P_{1/2}-3s3p^2\ ^4P_{1/2}$	4.89

to O IV density diagnostic based on the QS differential emission measure (QS-DEM) is presented in Section 3. The observational data set is presented in Section 4, and densities derived using the QS-DEM method. A modified method—referred to as the “log-linear DEM” method—that makes use of the  $\lambda 1343.51$  line is then developed that we recommend to use in the high-density regime ( $>10^{12}\text{ cm}^{-3}$ ). This method is then applied to derive densities for a series of flare kernel measurements in Section 6, and a final summary is given in Section 7.

## 2. Atomic Data and Line Modeling

The emission lines considered here are listed in Table 1. Those of Si IV are strong resonance transitions for which the intensity increases as  $N_e^2$ , while the O IV and S IV lines are intercombination transitions emitted from metastable levels. At low densities ( $\log N_e \lesssim 10$ ), the O IV and S IV lines behave as allowed transitions. However, eventually the density becomes high enough that electron collisional de-excitation dominates radiative decay in de-populating the levels. The intensities of the lines then increase only as  $N_e$ . This explains why the intercombination lines would be expected to become much weaker than the Si IV allowed transitions at high density, the basis for the Si IV–O IV density diagnostic.

The atomic models for O IV, Si IV, and S IV are taken from version 8.0 of the CHIANTI database (Del Zanna et al. 2015; Young et al. 2016). For Si IV, the observed energy levels are from the NIST database,<sup>7</sup> with radiative decay rates and electron collision strengths from Liang et al. (2009a) and Liang et al. (2009b). Energy levels for O IV are from Feuchtgruber et al. (1997) and the NIST database; for the three  $2s2p\ ^4P_j$  levels that give rise to lines in the *IRIS* wavebands, the energies are derived from the wavelengths of Sandlin et al. (1986)—see Polito et al. (2016). Radiative decay rates and electron collision strengths are from Liang et al. (2012). Energy levels for S IV are from the NIST database, and radiative decay rates are from Hibbert et al. (2002), Tayal (1999), Johnson et al. (1986), and an unpublished calculation of P.R. Young. Electron collision strengths are from Tayal (2000).

Equilibrium ionization fractions as a function of temperature are distributed with CHIANTI, and these are computed in the so-called “zero-density” approximation, assuming that ionization and recombination occur only from the ions’ ground states, and that the rates are independent of density. However, it is known that dielectronic recombination rates become suppressed at high density, and so in the present work, we modify the rates used in CHIANTI with the Nikolić et al. (2013) suppression factors. These lead to density-dependent

ion fractions, although for our work, we derive ion fraction tables as a function of pressure. Further details on the implementation are given in Young (2018).

In Table 1, the temperature of maximum ionization,  $T_{\max}$ , of an ion and the temperature of maximum emission,  $T_{\text{mem}}$ , of an emission line are given. We define the former to be the temperature at which the zero-density ionization fraction curve of the ion peaks. The latter is the temperature at which the contribution function for a specific emission line peaks. We define  $T_{\text{mem}}$  here by assuming a density of  $10^{12}\text{ cm}^{-3}$  and using the new ionization fraction curves computed at this density. The consequence of DR suppression is to push the ions to lower temperatures, and hence the values of  $T_{\text{mem}}$  are lower than those of  $T_{\max}$ . We also note that the  $T_{\text{mem}}$  value for  $\lambda 1343.51$  is significantly higher than for the other O IV lines, which is a consequence of it being a high excitation line.

Flare kernels usually show sudden large intensity increases and thus ionization equilibrium may be a questionable assumption. However, we note that previous authors have demonstrated that non-equilibrium effects are only important at relatively low densities and over short timescales. For example, Noci et al. (1989) considered non-equilibrium ionization for carbon ions in a coronal loop model that featured a steady siphon flow, and at loop densities  $>4 \times 10^9\text{ cm}^{-3}$  (significantly lower than the  $>10^{11}\text{ cm}^{-3}$  values considered here), the effects were small. Doyle et al. (2013) modeled the O IV and Si IV emission lines with an atomic model that fully incorporated density effects in the ion balance and found that O IV to Si IV line ratios in a transiently heated plasma reach their ionization equilibrium values within 10 s for a density of  $10^{10}\text{ cm}^{-3}$ . For higher densities, this time would be reduced further. Olluri et al. (2013) applied a sophisticated three-dimensional radiative magnetohydrodynamic model to the study of the O IV  $\lambda 1401.16/1404.78$  density diagnostic and found that non-equilibrium ionization results in O IV being formed over a wider range of temperatures than expected from the equilibrium ionization fractions. The low temperature contributions correspond to low heights in the atmosphere and thus higher densities. Therefore, the simulated ratios tend to correspond to higher densities than for the equilibrium case, and they do not represent the density at the  $T_{\max}$  of the ion. The range of densities over which O IV is sensitive to in this model is  $\log N_e = 8.2\text{--}10.5$ , and we emphasize again that this is much lower than the densities considered in the present work. If a high-density “knot” of plasma were present in this model, we would expect it to be in ionization equilibrium, and equilibrium diagnostics would apply. To summarize this discussion, we are justified in assuming ionization equilibrium for the high-density features studied in the present work.

We also assume that the measured line intensities come from a single structure when interpreting the line ratios. The effect of

<sup>7</sup> <https://www.nist.gov/pml/atomic-spectra-database>.

multiple structures with different densities (or pressures) on the interpretation of density diagnostics was considered by Doschek (1984) and Judge et al. (1997). In particular, the derived density of a high-density structure can be lower than the actual density if there is a significant amount of low density plasma in the instrument’s spatial resolving element. However, we consider this a relatively small effect for *IRIS* observations of flare kernels and bursts due to the high spatial resolution of *IRIS* and the fact that the densities of these features are two to three orders of magnitude higher than typical background active region plasma.

A further approximation used here is that particle distributions are described by Maxwellians. The effects of non-Maxwellians—in particular,  $\kappa$ -distributions—on the ratios of O IV to Si IV lines were studied by Dudík et al. (2014), who found that the O IV lines can be suppressed relative to Si IV by more than an order of magnitude as the  $\kappa$  index decreases from 10 to 2 (i.e., becoming less Maxwellian). However, for the high densities considered in the present work, we do not expect non-Maxwellian distributions to be maintained for periods long enough to affect the line intensities to any significant extent.

Adopting the above approximations, CHIANTI is used to model the intensities of the emission lines, and the method follows that of the companion paper Young (2018) in writing a line intensity,  $I$ , as a sum of isothermal components. We assume a given structure has constant pressure,  $P = N_e T$ , which is motivated by the consideration that the plasma will be trapped along field lines, and that the thickness of the transition region is significantly smaller than the pressure scale height at transition region temperatures. Hence,  $I$  is written as a function of pressure:

$$I(P) = \epsilon(X) \sum_k \frac{G(T_k, P) P^2 H(T_k) h_k}{T_k^2}, \quad (1)$$

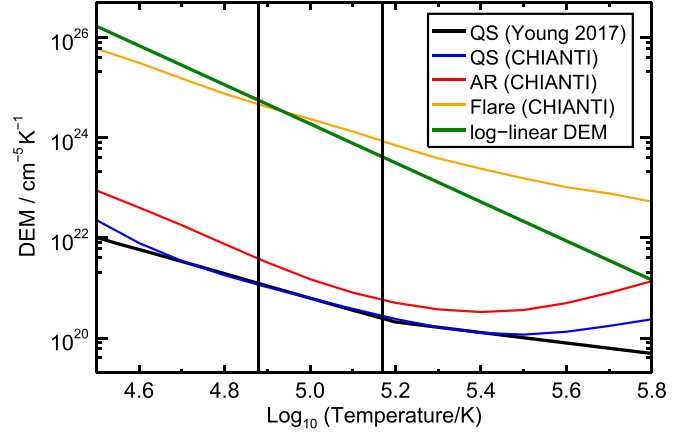
where  $\epsilon(X)$  is the abundance of the emitting element  $X$ ,  $G(T, P)$  is the contribution function,  $H(T)$  is the ratio of hydrogen to free electrons ( $N_H/N_e$ ), and  $h$  is the emitting column depth of the plasma. We calculate  $G$  using the CHIANTI software routine `gofnt.pro`, and  $H$  with the routine `proton_dens.pro`, which takes into account the element abundance and ionization fraction files. The sum is performed over a grid of temperatures,  $T_k$ , that have a spacing of 0.05 dex in  $\log T$  space.

The differential emission measure (DEM),  $\phi(T)$ , is related to  $h$  by the expression

$$\phi = \frac{P^2 H(T) h}{0.115 T^3}. \quad (2)$$

Note that the numerical factor in the denominator comes from  $\delta T = T \ln 10 \delta(\log T) = 0.115 T$ , where  $\delta T$  is the size of the temperature bin.

The assumption of constant pressure for the emission line modeling has the potential to cause confusion when referring to density diagnostics formed from two ions with different formation temperatures. For example, if the pressure is  $\log(P/\text{K cm}^{-3}) = 15$ , then the electron density at the  $T_{\max}$  value of Si IV is  $\log(N_e/\text{cm}^{-3}) = 10.12$ , but for O IV the density is  $\log(N_e/\text{cm}^{-3}) = 9.83$ . In the following text, we therefore refer to line ratio pressure diagnostics rather than density diagnostics. Where we refer to density, we will give the



**Figure 1.** Comparison of the QS DEM used in the present work (black line) with the QS, active region and flare (blue, red, and orange, respectively) DEMs available in CHIANTI, and the log-linear DEM (green) derived in Section 5. The vertical black lines show the  $T_{\max}$  values of Si IV and O IV.

quantity  $N_e^{\text{Si IV}}$ , which is the electron density at a temperature of  $\log(T/\text{K}) = 4.88$ , the  $T_{\max}$  of Si IV.

### 3. Emission Line Modeling

In this section, we derive pressure–ratio curves for various combinations of Si IV and O IV lines using a method that we refer to as the “QS-DEM method,” as it is based on the QS DEM. Each curve allows the user to convert a single observed line ratio directly to a pressure, and it is useful for the regime in which the O IV lines are no longer density sensitive ( $N_e \geq 10^{12} \text{ cm}^{-3}$ ), and when O IV  $\lambda 1343.5$  is unavailable.

Due to the separation in temperature of Si IV and O IV, it is necessary to make an assumption about the plasma temperature structure. Here, the DEM in the vicinity of the Si IV and O IV lines is assumed to take a universal shape that can be applied to any feature. This assumption fixes the relative values of  $h_k$  in Equation (1), and means that the ratio of any two emission lines depends solely on pressure.

Standard QS DEMs are available in the literature with perhaps the most well-known being the one distributed with the CHIANTI database. However, for our work we wish to systematically apply the pressure sensitive ion balance described in the previous section, which means generating the DEM curve with these results. For this purpose, we make use of results from the companion paper (Young 2018) that derived abundance ratios of magnesium to neon (Mg/Ne) and neon to oxygen (Ne/O) in the average QS. The latter is the most relevant, as the temperature range of the ions overlaps with the Si IV and O IV ions used here.

Young (2018) computed intensities using Equation (1) by assuming that  $h(T)$  takes a bilinear form such that there are three node points at  $\log T = 4.5$ ,  $5.2$ , and  $5.8$ , with values  $h = p_1$ ,  $p_2$  and  $p_3$ . The other values of  $h$  on the temperature grid are determined by linear interpolation in  $\log T - \log h$  space between  $p_1$  and  $p_2$ , and  $p_2$  and  $p_3$ . Thus, the function  $h(T)$  is defined entirely by  $p_{1,2,3}$ . A  $\chi^2$  minimization was then performed to reproduce the intensities of the six observed oxygen and neon line intensities by varying  $p_{1,2,3}$  and the Ne/O relative abundance. A standard QS pressure of  $10^{14.5} \text{ K cm}^{-3}$  was used.

The above procedure was applied to 24 QS CDS data sets obtained over the period 1996–1998. For the present work, we



**Table 2**  
Theoretical Ratios in Energy Units from the QS-DEM Method

	$\log(N_e^{\text{Si IV}}/\text{cm}^{-3})$										
Ratio	9.0	9.5	10.0	10.5	11.0	11.5	12.0	12.5	13.0	13.5	14.0
Si IV/O IV ratios											
$\lambda 1393.76/\lambda 1401.16$	7.45	7.59	7.79	8.64	11.74	21.29	50.72	143.6	437.8	1362.6	4221.3
$\lambda 1402.77/\lambda 1401.16$	3.73	3.80	3.90	4.33	5.88	10.67	25.42	71.99	219.5	682.9	2115.1
$\lambda 1402.77/\lambda 1343.51$	469.4	496.3	520.1	534.1	532.3	520.1	512.9	514.9	520.4	522.3	510.8
O IV/O IV ratios											
$\lambda 1401.16/\lambda 1343.51$	125.8	130.5	133.3	123.3	90.45	48.75	20.17	7.15	2.37	0.765	0.241
$\lambda 1399.78/\lambda 1401.16$	0.171	0.177	0.193	0.228	0.288	0.354	0.396	0.415	0.422	0.424	0.425
$\lambda 1404.78/\lambda 1401.16$	0.560	0.505	0.403	0.288	0.214	0.182	0.171	0.168	0.167	0.166	0.166
S IV/O IV ratios											
$\lambda 1404.83/\lambda 1401.16$	0.025	0.025	0.026	0.029	0.041	0.075	0.148	0.241	0.308	0.339	0.351

averaged the 24 sets of derived  $p_{1,2,3}$  values, giving  $p_1 = 3.93$ ,  $p_2 = 11.2$ , and  $p_3 = 166$  km. These values essentially define the QS DEM used in this section (noting the relation between  $\phi$  and  $h$  from Equation (2)), and the DEM values are plotted in Figure 1.

For the element abundances in Equation (1), we adopt the photospheric oxygen and silicon abundances of Caffau et al. (2011) and Lodders et al. (2009), respectively, but multiply the latter by a factor 1.6 to reflect the enhanced Mg/Ne abundance ratio found in the QS transition region by Young (2018). Silicon has a low first ionization potential (FIP), like magnesium, and so would be expected to be similarly enhanced compared to the high FIP element oxygen.

With the abundances and the column depths defined, we use a QS pressure of  $\log(P/\text{K cm}^{-3}) = 14.5$  to yield intensities for Si IV  $\lambda 1402.77$  and O IV  $\lambda 1401.16$  of 22.0 and 18.4  $\text{erg cm}^{-2} \text{s}^{-1} \text{sr}^{-1}$ , respectively. Doschek & Mariska (2001) measured a  $\lambda 1401.16/\lambda 1402.77$  ratio of  $0.267 \pm 0.050$  from QS spectra obtained by SUMER, which is a factor of 3.13 larger than the ratio predicted from the DEM. We consider this to be an *empirical correction factor* that is necessary to apply to the Si IV lines in order to address a well-known problem first highlighted by Dupree (1972). Specifically, the observed intensities of lines from the lithium- and sodium-like isoelectronic sequences are usually stronger than one would expect based on the emission measures from other sequences formed at the same temperature. This is why we apply the correction factor to the silicon lines and not those of oxygen.

Normalizing the ratio in this way was first undertaken by Feldman et al. (1977) for the analysis of *Skylab* spectra. It was also employed by Doschek et al. (2016) in a recent analysis of *IRIS* spectra, but not for other *IRIS* work (Peter et al. 2014; Gupta & Tripathi 2015; Kim et al. 2015; Yan et al. 2015; Polito et al. 2016).

With the empirical correction factor defined, the intensities of the Si IV, O IV, and S IV lines are computed with Equation (1) for a range of pressures using the  $h_k$  values from the QS analysis. We then take ratios of a selection of lines and present the results in Table 2, with two of the ratios displayed graphically in Figure 2. The  $\lambda 1393.76/\lambda 1401.16$  ratio can be directly compared to that given by Peter et al. (2014). Ratio values of 10 and 700 correspond to densities  $\log N_e^{\text{Si IV}} = 11.7$  and 13.3 in their work, compared to 10.8 and 13.2 here. The  $\lambda 1402.77/\lambda 1343.51$  ratio is insensitive to pressure, with an

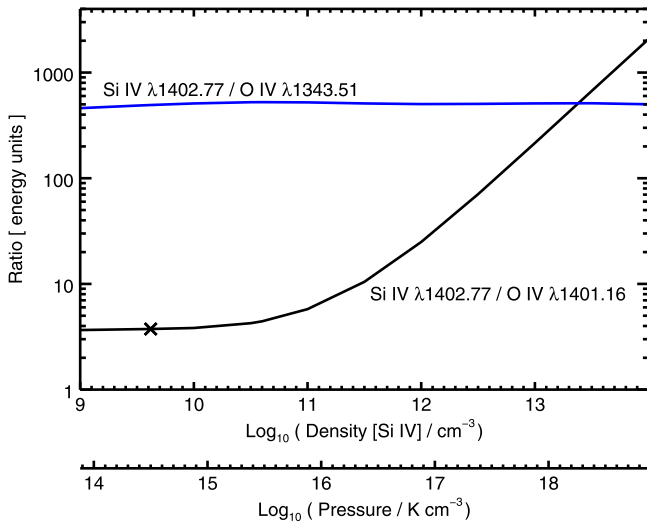
average value of 514 over a range of five orders of magnitude in pressure. This large ratio shows why the  $\lambda 1343.51$  is difficult to measure in *IRIS* observations: the noise level of the spectra is around 10 DN (data numbers), and the maximum signal is about 16000 DN before saturating. Thus  $\lambda 1343.51$  only becomes measurable when  $\lambda 1402.77$  is close to saturation.

Finally, in this section, we return to two of the assumptions that were made for the modeling described above; specifically the element abundances and shape of the DEM curve. Our method assumes that the events have a Si/O abundance ratio that is consistent with the small FIP enhancement factor found by Young (2018). The two *IRIS* features that we know have high densities are flare kernels (an example is studied here) and UV bursts, which are compact, intense brightenings seen in active regions but not related to flares (the bomb events studied by Peter et al. 2014, are examples). Both of these features are highly impulsive, and we note that Warren et al. (2016) recently found that impulsive active region heating events show close-to photospheric abundances.

The suitability of using a QS DEM for UV bursts was discussed in detail by Doschek et al. (2016) with reference to *Skylab* spectra from which a much wider range of emission lines was available. They concluded that the shape of the QS DEM in the vicinity of the Si IV and O IV ions is approximately the same in active regions in an average sense, and that the variations in the Si IV/O IV ratio across an active region are driven largely by density variations rather than those in temperature or DEM. This is borne out by a comparison of the Young (2018) QS DEM with the QS, active region and flare DEMs available in the CHIANTI database (Figure 1). Without additional ions in the *IRIS* data sets to derive DEMs for UV bursts and flare kernels, we feel justified in using the QS DEM here.

#### 4. Observations and Measurements

*IRIS* is described in detail by De Pontieu et al. (2014), and hence here we only briefly summarize the important features relevant to the present work. A single telescope feeds a spectrograph and slitjaw imager (SJI), allowing simultaneous imaging and slit spectroscopy. Spectra are obtained in three wavelength bands, and the lines studied in the present work are from the far-ultraviolet wavebands 1331.7–1358.4 and 1389.0–1407.0 Å (FUV1 and FUV2, respectively). The



**Figure 2.** Si IV/O IV ratio–density curves predicted from the QS-DEM method. These are plotted as a function of the density at  $\log T = 4.88$ .

spectral resolution is about 53000 and the spatial resolution is  $0''.33$ .

The observations are from active region AR 12192, one of the best known of Solar Cycle 24 due to its very large sunspot, and the high number of confined flares it produced during its transit across the solar disk during 2014 October 17–30. The *IRIS* observation that began at 20:52 UT on October 24 is used and it consisted of a 6.75 hr sit-and-stare data set that captured a long-duration X3.1 flare, which peaked at 21:41 UT. Our interest here lies with the rise phase of the flare when the *IRIS* slit lay across one of the developing ribbons, and three SJI images of the ribbon are shown in Figure 3. This ribbon had a complex shape and time evolution, and it produced intense flare kernels in Si IV at two locations, namely  $Y = -295''$  during 21:11–21:18 UT, and  $Y = -330''$  during 21:25 to 21:28 UT. The observational sequence began with 15 s exposure times, but at 21:11:18 UT exposure control was triggered, resulting in sub-second exposures for the period up to 21:36:41 UT. These enabled unsaturated profiles of the strong Si IV  $\lambda 1402.77$  line to be obtained. In the following text, we will refer to spectra obtained from specific exposures, and we will use the shorthand notation ExpNN to refer to exposure number NN.

The data set used here is a level-2 one downloaded from the Hinode Science Data Center Europe (<http://sdc.uio.no>) and was processed with version 1.83 of the *IRIS* level 1 to level 1.5 pipeline. Spectra derived from each exposure are averaged across a few pixels along the slit and version 4 of the *IRIS* radiometric calibration was applied. Gaussian profiles were fit to the emission lines in the spectra using the IDL routine `spec_gauss_iris`. Wavelength calibration was performed by measuring the O I  $\lambda 1355.60$  and Si I  $\lambda 1401.51$  lines and assuming they are at rest in the spectra. The offsets were then applied to all other lines in the FUV1 and FUV2 channels. To derive Doppler shifts, the rest wavelengths were taken from the line list available at [http://pyoung.org/iris/iris\\_line\\_list.pdf](http://pyoung.org/iris/iris_line_list.pdf).

Our first test of the QS-DEM method is to consider a compact brightening seen in Exp38 (21:02:45 UT). From the SJI 1330 Å images, the brightening appears to belong to a loop, although this is spatially aligned almost exactly to the flare ribbon that

appears about 10 minutes later. Thus, the feature may represent early energy input to the flare ribbon. The brightening lasts for about 2 minutes and the peak intensity occurs in Exp36, but  $\lambda 1402.77$  is saturated in this and the following exposure. For Exp38, pixels 225 to 227 along the slit were averaged, and Gaussian fit parameters for the emission lines are given in Table 3. The observed O IV  $\lambda 1399.78/\lambda 1401.16$  ratio of  $0.394 \pm 0.016$  is just below the high-density limit and yields a density of  $\log N_e^{\text{Si IV}} = 11.96_{-0.22}^{+0.35}$  using data from Table 2, while  $\lambda 1402.77/\lambda 1401.16$  is  $32.4 \pm 0.5$ , indicating  $\log N_e^{\text{Si IV}} = 12.13 \pm 0.01$ . The results in Table 3 may also be used to predict that  $(\text{Si IV } \lambda 1404.83 + \text{O IV } \lambda 1404.78)/\lambda 1401.16$  should be  $0.319$  at  $\log N_e^{\text{Si IV}} = 12.0$ , which is close to the observed ratio of  $0.36 \pm 0.01$ . (Note that the uncertainties quoted here are the statistical uncertainties arising from the Gaussian fitting, and do not include atomic data, element abundance and DEM uncertainties which are likely to be at least 20%.) We conclude that the QS-DEM method for computing the theoretical  $\lambda 1402.77/\lambda 1401.16$  ratio thus provides good agreement with observed line intensities for this high-density feature.

Now we consider flare kernel spectra from exposures 69 and 70, which mark the onset of exposure control. Exp69 (21:11:08 UT) has a 15 s exposure time and clearly displays the O IV lines, including  $\lambda 1343.51$ , but Si IV  $\lambda 1402.77$  is saturated, preventing an accurate intensity measurement (see Appendix). The exposure time drops to 0.44 s for Exp70 (21:11:18 UT) and an unsaturated Si IV line is detected together with very weak O IV  $\lambda 1401.16$ , but O IV  $\lambda 1343.51$  cannot be identified. Gaussian fits were performed to the O IV lines from Exp69, plus O IV  $\lambda 1401.16$  and Si IV  $\lambda 1402.77$  from Exp70 (Figure 4), while the blend of O IV  $\lambda 1404.78$  and Si IV  $\lambda 1404.83$  is also measured. For Exp69, pixels 219 to 221 along the slit were averaged, and 218 to 220 for Exp 70, the difference due to the rapid southward motion of the flare ribbon. Gaussians were fit to each line, and Table 3 gives the centroids, line-of-sight velocities, full-widths at half-maximum and integrated intensities. Due to uncertainties in establishing the spectrum background for O IV  $\lambda 1343.51$ , the intensity error was increased by  $\sqrt{2}$ .

The weak O IV  $\lambda 1401.16$  line in the Exp70 spectrum was used to provide a correction factor for Si IV  $\lambda 1402.77$  as this is saturated in Exp69; the O IV intensity was found to have changed by a factor  $0.75 \pm 0.18$  between Exp69 and Exp70. Hence we divide the Exp70  $\lambda 1402.77$  intensity by this factor (see Table 3) to obtain a value that may be directly compared with the O IV Exp69 measurements. However, we note that the error bars become rather large.

The O IV  $\lambda 1399.78/\lambda 1401.16$  observed ratio is  $0.47 \pm 0.02$ , which is greater than the high-density limit (Table 2). Thus, we are in the high-density regime where the diagnostic is no longer useful. The  $\lambda 1402.77/\lambda 1401.16$  ratio is  $195 \pm 62$ , which yields  $\log N_e^{\text{Si IV}} = 12.96_{-0.12}^{+0.09}$  from Table 2, while  $\lambda 1402.77/\lambda 1343.51$  is  $1327 \pm 367$ , significantly larger than the theoretical value from Table 2. We also note that  $(\text{Si IV } \lambda 1404.83 + \text{O IV } \lambda 1404.78)/(\text{O IV } \lambda 1401.16)$  has a measured value of  $0.78 \pm 0.02$ , yet the theoretical ratio is lower than this at all densities. For example, at  $\log N_e^{\text{Si IV}} = 13.0$  the ratio is 0.47. As the intensity of O IV  $\lambda 1404.78$  is known to be consistent with the other O IV lines (e.g., Keenan et al. 2002), the observed Si IV  $\lambda 1404.83$  line must be about a factor of two stronger than the QS-DEM method predicts.

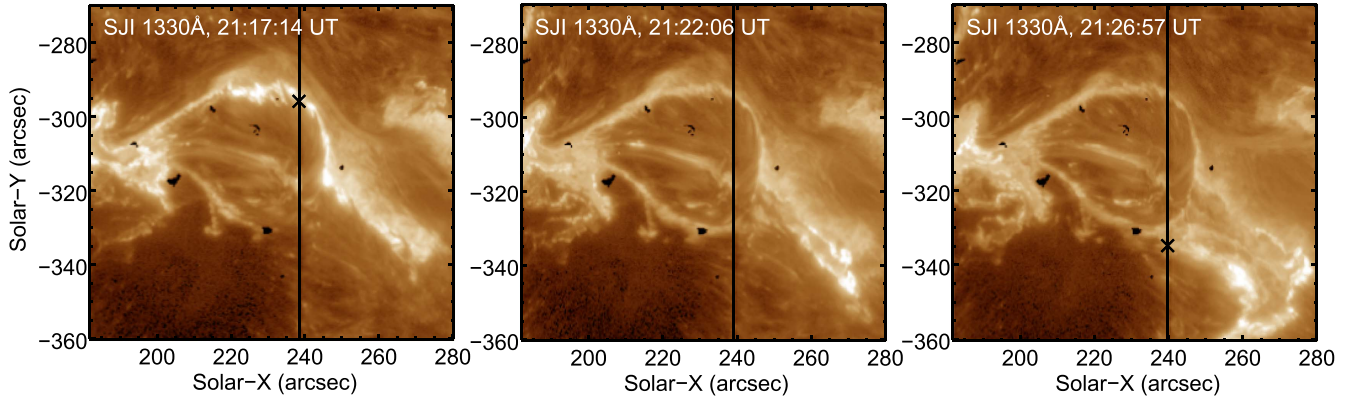
**Table 3**  
Emission Line Parameters

Ion	Line	Wavelength	Velocity	FWHM	Intensity	Exposure
Flare kernel						
Si IV	$\lambda 1402.77$	$1402.795 \pm 0.009$	$5.3 \pm 2.0$	$24.6 \pm 0.1$	$328,700 \pm 1500$	70
	...	...	...	...	$438,800 \pm 104,300^a$	69
O IV	$\lambda 1343.51$	$1343.559 \pm 0.010$	$10.5 \pm 2.2$	$27.9 \pm 2.8$	$331 \pm 47$	69
	$\lambda 1399.78$	$1399.791 \pm 0.010$	$5.4 \pm 2.0$	$31.4 \pm 1.3$	$1051 \pm 44$	69
	$\lambda 1401.16$	$1401.188 \pm 0.009$	$6.5 \pm 2.0$	$30.0 \pm 0.3$	$2251 \pm 26$	69
		$1401.205 \pm 0.017$	$10.1 \pm 3.6$	$31.2 \pm 7.4$	$1686 \pm 401$	70
S IV	$\lambda 1404.81$	$1404.843 \pm 0.009$	$3.6 \pm 2.0$	$28.4 \pm 0.4$	$1754 \pm 26^b$	69
Bright point						
Si IV	$\lambda 1402.77$	$1402.775 \pm 0.009$	$1.1 \pm 2.0$	$17.3 \pm 0.0$	$36,069 \pm 84$	38
O IV	$\lambda 1399.78$	$1399.784 \pm 0.009$	$3.9 \pm 2.0$	$22.3 \pm 0.8$	$438 \pm 17$	38
	$\lambda 1401.16$	$1401.170 \pm 0.009$	$2.5 \pm 2.0$	$22.4 \pm 0.3$	$1112 \pm 17$	38
S IV	$\lambda 1404.83$	$1404.821 \pm 0.009$	$-1.0 \pm 2.0$	$23.7 \pm 0.8$	$401 \pm 13^b$	38

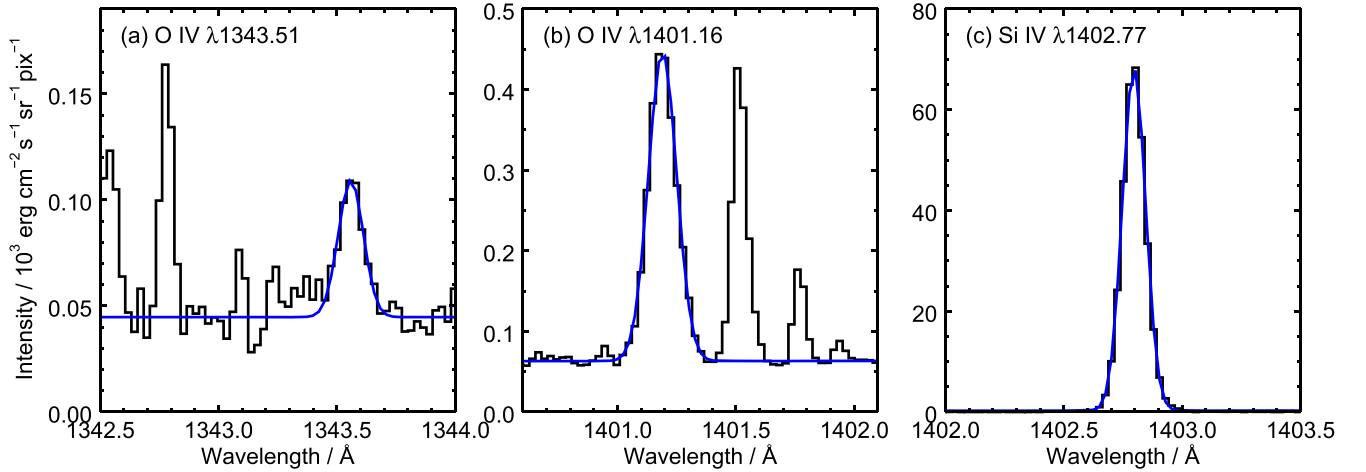
**Notes.**

<sup>a</sup> Intensity scaled from the Exp70 measurement—see the main text.

<sup>b</sup> Blended with O IV  $\lambda 1404.78$ . Parameters derived for the blended feature.



**Figure 3.** Images of the flare ribbon obtained with the *IRIS* SJI 1330 Å filter. The location of the *IRIS* slit is marked with a vertical black line, and the two spatial locations studied are marked with crosses in the left and right panels.



**Figure 4.** Flare kernel spectra and Gaussian fits for Exp69 (panels (a) and (b)) and Exp70 (panel (c)).

**Table 4**  
Theoretical Ratios in Energy Units from the Log-linear DEM Method

Ratio	$\log(N_e^{\text{Si IV}}/\text{cm}^{-3})$										
	9.0	9.5	10.0	10.5	11.0	11.5	12.0	12.5	13.0	13.5	14.0
Si IV/O IV ratios											
$\lambda 1393.76/\lambda 1401.16$	17.17	17.20	17.40	19.28	26.47	48.60	116.2	325.7	974.1	2965.6	8985.6
$\lambda 1402.77/\lambda 1401.16$	8.61	8.63	8.73	9.67	13.28	24.38	58.31	163.4	488.7	1487.8	4506.6
$\lambda 1402.77/\lambda 1343.51$	1478.4	1530.2	1563.2	1557.0	1497.6	1413.8	1354.6	1326.1	1308.4	1282.7	1224.4
O IV/O IV ratios											
$\lambda 1401.16/\lambda 1343.51$	171.7	177.4	179.1	161.0	112.8	57.98	23.23	8.115	2.677	0.862	0.272
$\lambda 1399.78/\lambda 1401.16$	0.172	0.179	0.197	0.236	0.299	0.362	0.401	0.417	0.423	0.425	0.425
$\lambda 1404.78/\lambda 1401.16$	0.555	0.494	0.386	0.274	0.207	0.180	0.170	0.167	0.167	0.166	0.166
S IV/O IV ratios											
$\lambda 1404.83/\lambda 1401.16$	0.051	0.051	0.052	0.060	0.087	0.162	0.315	0.500	0.623	0.677	0.699

The above results demonstrate some failings of the QS-DEM method for the high-density regime. Hence, the next step is to modify the DEM by making use of the extra information provided by O IV  $\lambda 1343.51$ .

### 5. An Updated Diagnostic Using O IV $\lambda 1343$

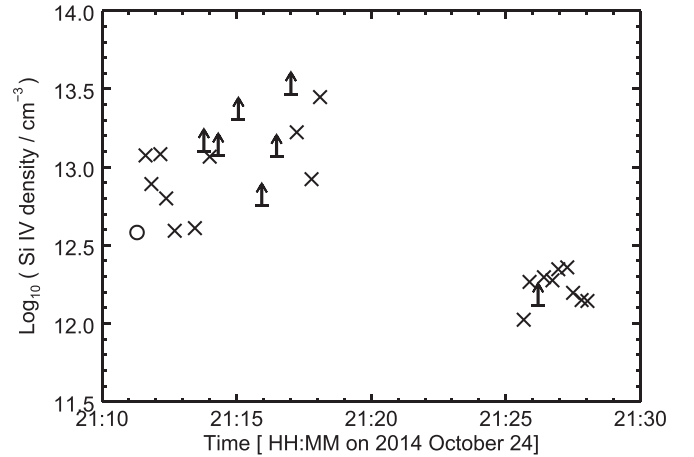
Section 3 showed how a set of pressure–ratio curves could be derived for various combinations of O IV, Si IV, and S IV lines using only the assumptions of a fixed shape to the DEM and a particular set of element abundances. Comparing with line intensities from the 2014 October 24 flare kernel, we find two discrepancies: (1) O IV  $\lambda 1343.51$  is predicted to be too strong by about a factor two, and (2) S IV  $\lambda 1404.81$  is predicted to be too weak by a similar amount. Can we create a new model that fixes these discrepancies?

Our procedure, which we refer to as the “log-linear DEM method,” is to define a new DEM by  $\log \phi = a + b \log T$ , and then use the measured intensities of  $\lambda 1402.77$ ,  $\lambda 1401.16$ , and  $\lambda 1343.51$  to solve Equation (1) for the three lines and yield  $P$ ,  $a$ , and  $b$ . Using the flare kernel intensities from Table 2, we derive  $a = 43.78$ ,  $b = -3.90$ , and  $\log(P/K \text{ cm}^{-3}) = 17.46$ . The latter implies  $\log N_e^{\text{Si IV}} = 12.58$ , which is 0.38 dex lower than that derived from the QS-DEM method.

If we now treat this DEM as a universal DEM, then new pressure–ratio curves can be derived, and these are tabulated in Table 4. By definition, the new DEM fixes the problem with  $\lambda 1343.51$  noted for the QS-DEM method. We also find that the  $(\text{S IV } \lambda 1404.83 + \text{O IV } \lambda 1404.78)/(\text{O IV } \lambda 1401.16)$  ratio is predicted to be 0.69, significantly closer to the observed ratio of  $0.78 \pm 0.02$  than that from the QS-DEM method.

### 6. Application to Flare Kernels

From the theoretical  $\lambda 1402.77/\lambda 1401.16$  line ratio in Table 4, we can now derive densities for the two sequences of flare kernel measurements highlighted earlier (see Figure 3). The first sequence occurred from 21:11 to 21:18 UT at approximately slit pixel 215, and the second from 21:25 to 21:28 UT at pixel 98. Kernels at the former position were around an order of magnitude more intense in the Si IV line. For selected exposures, spectra were averaged over three to five pixels in the slit direction, and the two emission lines were fit with Gaussians. Only an upper limit to the O IV intensity could be made for some exposures. Intensity ratios were then



**Figure 5.** Flare kernel densities for the 2014 October 24 data set, derived with the log-linear DEM method. The circle corresponds to Exp70 (Table 3), and arrows indicate lower limits due to very weak O IV emission.

converted to  $N_e^{\text{Si IV}}$  values using the data from Table 4, and the results are plotted in Figure 5.

The kernels at the first position show a wide spread in density, which is mostly due to large variability in the Si IV intensity, which has values ranging from  $3.3 \times 10^5 \text{ erg cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$  at Exp70 to  $6.8 \times 10^6 \text{ erg cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$  at Exp75, with changes between exposures of up to a factor of two (for example, between exposures 78 and 79). We note that during the exposure control period the FUV channel exposure times were  $<0.5 \text{ s}$ , while the average cadence was 16.2 s. Thus the *IRIS* intensities represent brief snapshots in the wider evolution of the flare ribbon. The large intensity variation suggests that we are observing multiple, short-lived energy input events at the spatial location rather than the evolution of single event. We note that recent modeling efforts for flare kernels have suggested they consist of many structures below the resolution limit of *IRIS* (Reep et al. 2016).

The Si IV intensity at the second location is more stable, and the corresponding density variation is smaller. This location is at the end of a hairpin shape in the flare ribbon, which can be seen in the bottom right corners of the middle and right panels of Figure 3. The more uniform intensity suggests that the brightening may belong to a single energy input event, unlike the earlier observation.



## 7. Summary and Recommendation

The aim of the present work has been to create a model for the variations of ratios of Si IV to O IV emission lines in the *IRIS* spectra that will allow users to derive densities in the high-density regime of  $N_e \geq 10^{12} \text{ cm}^{-3}$ . Two approaches were adopted that differed in how the temperature structure in the atmosphere was modeled. The first was to assume that a QS DEM can be applied to all solar features, and checks against a spectrum for which the density is close to the high-density limit of the O IV  $\lambda 1399.78/\lambda 1401.16$  ratio showed good agreement. However, the method failed to reproduce the strength of the O IV  $\lambda 1343.51$  line and the O IV  $\lambda 1404.78 + \text{Si IV } \lambda 1404.81$  blend in a higher-density flare kernel spectrum.

A second method, referred to as the log-linear DEM method, made use of O IV  $\lambda 1343.51$  in combination with Si IV  $\lambda 1402.77$  and O IV  $\lambda 1401.16$  to define a DEM that is linear in  $\log T - \log \phi$  space over the region of formation of the ions. We took advantage of a special flare kernel data set for which the exposure time dropped by a factor of 34 between two exposures, allowing good measurements of all three emission lines. This method yields lower densities than the QS-DEM one by about 0.4 dex and is also better able to reproduce the intensity of the O IV  $\lambda 1404.78 + \text{Si IV } \lambda 1404.81$  blend. Our recommendation is that the ratio curves from the log-linear DEM method (tabulated in Table 4) be treated as universal curves to be applied for any case where the O IV density diagnostic has reached its high-density limit. For densities below this, the QS-DEM method seems to be more appropriate and has the advantage that it tends to the correct QS density value.

The log-linear method was then applied to two sequences of flare ribbon observations from the 2014 October 24 X-flare, and densities were derived. At one location of intense, variable activity the densities were found to lie between  $10^{12.5}$  and  $10^{13.5} \text{ cm}^{-3}$ . A second location with weaker, more steady activity showed densities of around  $10^{12.3} \text{ cm}^{-3}$ . We note that these densities were derived assuming a constant pressure atmosphere and apply at the temperature of  $\log T = 4.88$ .

It is important to caution that the two diagnostic methods are best used for flare kernels and UV bursts. We know of at least one example of a structure for which the two methods will fail, and this is the sunspot plume. These structures have been studied by Straus et al. (2015) and Chitta et al. (2016) and they can show O IV  $\lambda 1401.16$  intensities that are comparable to Si IV  $\lambda 1402.77$  and are thus not compatible with the ratio curves from Tables 2 and 4. This is likely due to a quite different temperature structure, and possibly also abundance anomalies.

We also caution that the methods are not intended to be used for high-precision density measurements. A simple translation of measurement errors to density uncertainties will generally yield very small errors on the density, but there are very significant uncertainties associated with the assumptions of the method: atomic data, the shape of the DEM, and element abundances. A more realistic uncertainty is probably a factor of two. However, the ratio curves do provide a baseline for comparing different types of feature seen in *IRIS* data.

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*Facility:* *IRIS*.

*Software:* Solarsoft, CHIANTI.

## Appendix

### Saturated Pixels for the FUV Spectral Channel

As noted in the main text, the Si IV lines often become saturated during observations of flare kernels and UV bursts. For density diagnostics, we simply need the integrated intensity of an emission line. Can an accurate intensity be recovered from the saturated line profiles?

Saturation occurs when the signal from the CCD, in terms of numbers of electrons, is too high for the analog-to-digital convertor (ADC). For the *IRIS* cameras, the saturation limit is 16283 DN. The gain for the FUV camera is set to 6 electrons  $\text{DN}^{-1}$ , and thus a signal of 98000 electrons from a single pixel will reach the ADC saturation threshold.

The *IRIS* CCDs have a full well of 150,000 electrons (De Pontieu et al. 2014), and therefore a photon flux for a single pixel that results in an electron count between 98000 and 150,000 electrons cannot be accurately counted by the ADC. Above 150,000 electrons, blooming will occur, whereby charge spills into neighboring pixels. If the neighboring pixels remain below the 98000 electron threshold, then the overspill charge can be accurately measured.

Note that if pixel binning is performed by the camera, then the situation becomes worse. For example, for  $2 \times 2$  binning (which was used for the 2014 October 24 flare event studied here) the ADC threshold for the binned pixel remains at 98000 electrons, whereas the effective full well capacity becomes 600,000 electrons. Thus, any signal between these two numbers is effectively lost.

To summarize, summing the intensity across the profile of a saturated emission line will likely significantly underestimate the actual intensity of the line.

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